AP CALCULUS SUMMER ASSIGNMENT

Hello Future AP Calculus Students!!!

The following is a sampling of precalculus topics that will be used throughout the course. Students strong in the knowledge of these topics typically have an easier time throughout the course. Because there will be no time to review in the fall, it is up to you to assess your own understanding of these before returning in August. To be successful in this course, you must have a strong intuitive understanding of these topics and be able to apply these skills to the many new concepts you will be learning. You will find that AP Calculus is unlike any math class you have taken before. You will need every math concept you have learned up to now – forgetting is not an option or an excuse acceptable in this course. Every concept will also build on the previous one, so you cannot let yourself ever fall behind.

The next few pages consist of an overview of the predominant precalculus topics (not all of course, but some of the most important!), a brief reminder of how to approach various topics, and some problems to help you assess your understanding of these topics. None of this material should be unfamiliar to you, but it needs to be fresh in your mind before returning in the fall. I especially want to stress that you should have key concepts like the unit circle and trigonometric identities MEMORIZED!!

*This assignment will be collected the first day of class and there will be a QUIZ on this material on day 3 *

SAMPLE:

Trigonometry: Everything will be done in radians

Unit Circle!! You MUST know the 6 trig values of the unit circle very well. .

Ex. Sin $(2\pi/3)$

 $\tan (7\pi/6)$

 $\cos (7\pi/4)$

 $\sin(\pi/2)$

Graphs of all 6 trig functions - including domain, range, and period.

Identities: Pythagorean, double angle, sum and difference, even/odd

Solving Equations with trig (will need identities and unit circle)

Ex. $\cos 2x + \sin^2 x = 0$ (all real x)

 $2\sin^2 x = 3\sin x - 1 \ 0 < x < 2\pi$

Graphical Analysis

Determine domain and range of function

Ex.
$$Y = \sqrt{6-x}$$
 $y = \frac{(x-3)(x+6)}{x^2-5x+6}$ $y = \log(3x-4)$

Translations and scale changes

Ex. Given the graph of f(x), be able to graph f(x+2), 3f(x), f(-x), f(|x|), etc

Graphs of "toolkit" functions including all domain and range

Ex.
$$Y = x^2$$
 $y = x^3$ $y = \sqrt{x}$ $y = \ln x$ $y = 3^x$ $y = \frac{1}{x}$

Solving Equations and inequalities

Finding inverses of functions (including trig)

Logarithms and exponentials: MUST know properties and how to use in solving equations

Ex. Solve:
$$2\ln (x-2) - \ln (x) = \ln (2)$$

Solve: $e^{3\ln x - \ln 2} = 4$

Test Point Method to solve polynomial and rational inequalities. Express solutions in interval notation.

Ex. Solve:
$$x^2(x-6)(x^2-9) > 0$$
 Solve: $\frac{(x+2)(x-1)^3}{(x+4)^2} < 0$

Solving ALL types of equations – log, exponential, trig, rational, polynomial, radical, etc.

Solutions:
$$(40 \ 2X \ app \ | 4S \ pq \ | 1)$$
Sin $(2\pi/3) = \frac{\sqrt{3}}{2}$ tan $(7\pi/6) = \frac{\sqrt{3}}{3}$ cos $(7\pi/4) = \frac{\sqrt{3}}{2}$ sin $(\pi/2) = 1$
Sin $(2x) = 2S^{1/2} \times Cos \times X$
Sin $(x) = 2S^{1/2} \times Cos \times X$
Sin $(x) = -5/n \times X$
Cos $(2x) = Cos \times X$
Sin $(x) = -5/n \times X$
Cos $(2x) = Cos \times X$
Sin $(x) = 2S^{1/2} \times X$
Solve:

Solve:

Solve:

2sin $(x + y) = Cos \times X$
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Notes that might help (

Solving Polynomial & Kational Mequalities

- Set Inequality to zero.

- Put zeros of numerator + denominator on # line

- check values within each interval to see if positive or regative

- choose intervals want = write in interval notation

Ex.
$$\chi^3 - 5\chi^2 \angle 6\chi$$
 $\chi^3 - 5\chi^2 - 6\chi \angle 0$
 $\chi(\chi - 6\chi \chi + 1\chi \bigcirc 0)$
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* signs will alternate unless have even roofs

Ex. $(x-2)^2(x+4)(x-4)^3(x-1)^4 \ge 0$ (|a|ways put 2 lines 11 jukan even 10)

+ If doesn't factor, graph on calculator to find zeros

* Used in solving any polynomial or rational meq. Sometimes need with

Ex. Determine the domain of $y=\sqrt{\frac{x^2-4}{x+3}}$.

- Remember $\frac{x^2-4}{x+3} \ge 0 + x+3 \ne 0$ to be in domain: $\frac{-1}{x+3} + \frac{1}{x+3} = \frac$

FRAPHS y=f(x) $y=f(x+c) \Rightarrow moves left c$ $y=f(x-c) \Rightarrow moves rf c$ $y=f(x)+c \Rightarrow moves vp c$ $y=f(x)-c \Rightarrow down c$

 $y=Kf(x) \Rightarrow mu|f. \ y's by k$ $y=f(kx) \Rightarrow mu|f. \ x's by \frac{1}{k}$ $y=-f(x) \Rightarrow reflects over y-axis$ $y=f(-x) \Rightarrow reflects over y-axis$ $y=f(x) \Rightarrow all y values are positive$ $y=f(x) \Rightarrow all neg. x values have sare y values

<math>y=f(x) \Rightarrow all neg. x values are y values$

Inverses

To find $f^{-1}(x)$, switch $x+y \neq solve$ for y.

Pomember, domain of f(x) = range of $f^{-1}(x) \neq v$ ice versa

Ex. Find the inverse of $f(x) = \sqrt[3]{x-2} + 6$. Ex. $f(x) = \frac{2x+1}{x-2}$. Find $f^{-1}(x)$ $x = \sqrt[3]{y-2} + 6$ $x = \sqrt[3]{y-2}$ $(x-6)^3 = y-2$ $(x-6)^3 = y-2$ (

Ex. Solve 3x-2=6. Ex. Solve log (x71)+log x = 1096[X(4+1]=1 In 3x-2= In 6 x(x+1)=6 (y-2)/n3=/n6 X2+X=6 X2+X-6=0 (X+3)(x-2)=0 Ex. Solve 6e2 4 In original egn. Can't take log of reg! In (e2x)=In 3 2x= ln 2/3 - Use propertus of loss to combine exp. ← Exp. bace 3+log3 cancel 6/c invertes x4=8 (x=4/8

I RIGEOS.

Y MUST know unit circle values extremely well.

Y Know identities!

Ex. $2\sin^2 x - 1 = 0$ $0 \le x \le 2\pi$ Ex. $3\sin^2 x + 2\sin 0 \cos 0 = 0$ $3\sin^2 x = \frac{1}{2}$ $3\sin^2 x = \frac{1}{2}$